Performance Evaluation of Parallel Sparse Matrix-Vector Products on SGI Altix3700

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Outline

- Introduction
- Sparse Matrix-Vector Product
- SGI Altix3700
 NUMA architecture
 - First-touch mechanism
- Experiments
 - Sparse matrix-vector product
- Conversion costs
- Conclusions

Introduction (1)



- Demands for reliable and portable parallel numerical libraries are growing.
- Scalable Software Infrastructure Project
 Started as a 5-year national projects since
 - Nov. 2002. – Development
 - Portable implementation of the following libraries:
 - Portable implementation
 Parallel eigen solvers
 - Parallel linear system solvers
 - Parallel fast integral transforms

Introduction (2)

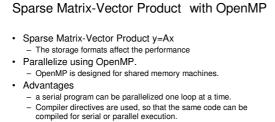
- We are planning to develop a library of iterative solvers, which includes a wide range of iterative solvers, preconditioners, and storage formats.
- The matrix-vector product is the most important kernel operation for iterative linear solvers.
- Its performance has a significant effect on the performance of linear solvers.

Introduction (3)

- We discuss the performance of sparse matrix-vector products on a cc-NUMA machine SGI Altix3700.
- · What's problems :
 - First-touch mechanism
 - The performance of sparse matrix-vector product for each storage format.
 - conversion costs of the storage format.

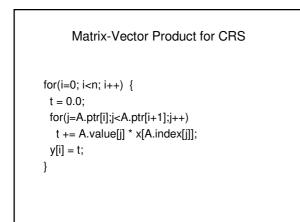
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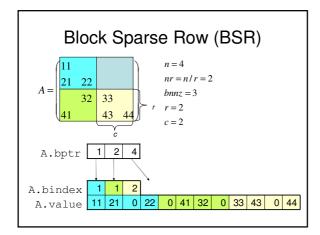
- compiled for serial or parallel execution. - portability
- Special treatment for data locality, such as first-touch, may be required, especially for cc-NUMA architectures (will be discussed later).

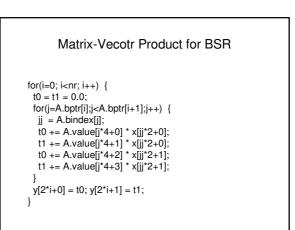
Compressed Row Storage (CRS) 11 n = 421 22 A =nnz = 832 33 41 43 44 1 2 4 6 9 A.ptr A.index 1 1 2 2 3 1 3 4 A.value 11 21 22 32 33 41 43 44

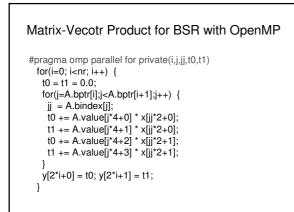


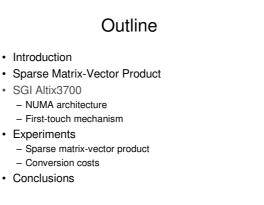
Matrix-Vector Product for CRS with OpenMP

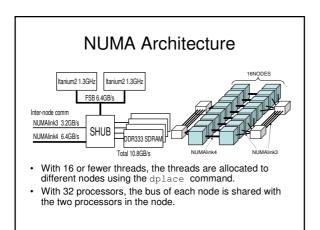
```
#pragma omp parallel for private(i,j,t)
for(i=0; i<n; i++) {
    t = 0.0;
    for(j=A.ptr[i];j<A.ptr[i+1];j++)
    t += A.value[j] * x[A.index[j]];
    y[i] = t;
}</pre>
```

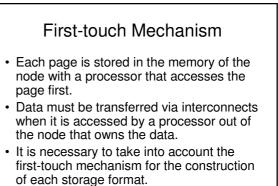


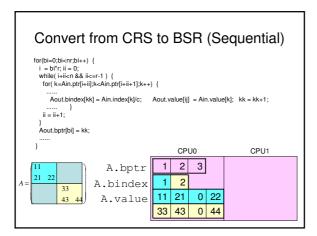


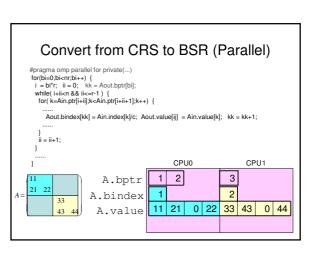


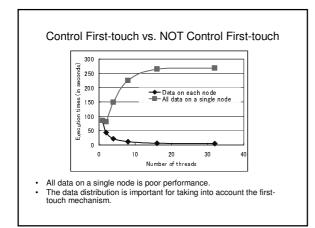






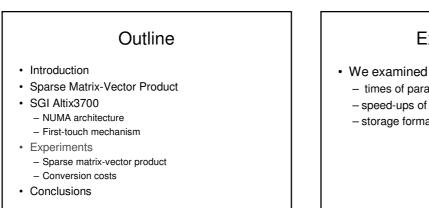








- In order to obtain good performance, each page should be assigned to the node with the processor that most often accesses the page.
- To control first-touch, we parallelized the storage format conversion routines.



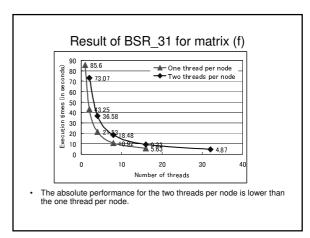
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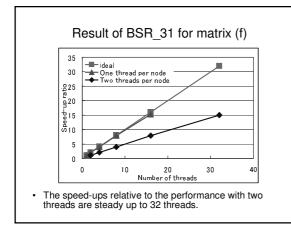
- times of parallel matrix-vector products
- speed-ups of parallel matrix-vector products
- storage format conversion costs

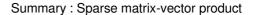
	Name	Dimension	Nonzeros	Ave.			
(a)	af23560	23,560	484,256	20.55			
(b)	fidapm37	9,152	765,944	83.69			
(C)	fidap011	16,614	1,091,362	65.69			
(d)	bcsstk30	28,924	2,043,492	70.65			
(e)	s3dkq4m2	90,449	4,820,891	53.30			
(f)	Poisson	1,000,000	26,463,592	26.46			
 (a) to (e) : Matrix Market. (f) : FEM of the three-dimensional Poisson equation on a cube. Ave : The average number of the non-zero elements per row. 							

Execution times (in seconds) of 1000 iterations							
Number	of threads	1	2	4	8	16	32
Matrix	Format					10	
(-)	CRS	3.79	1.89	0.91	0.46	0.24	0.14
(a)	BSR_41	1.46	0.72	0.28	0.15	0.09	0.07
(1-)	CRS	2.53	1.33	0.63	0.32	0.18	0.10
(b)	BSR_22	2.24	1.19	0.57	0.24	0.14	0.09
(-)	CRS	3.87	1.98	1.01	0.48	0.26	0.15
(C)	BSR_41	2.51	1.30	0.65	0.24	0.13	0.09
(-1)	CRS	6.81	3.53	1.88	0.97	0.46	0.24
(d)	BSR_41	4.48	2.34	1.30	0.61	0.23	0.14
	CRS	20.87	10.47	5.26	2.71	1.43	0.68
(e)	BSR_41	9.17	4.65	2.39	1.30	0.62	0.27
(f)	CRS	149.50	74.96	37.43	18.76	9.51	4.97
	BSR_31	85.60	43.25	21.53	10.92	5.63	4.87
	DIA	178.50	89.19	44.34	16.40	4.72	2.81

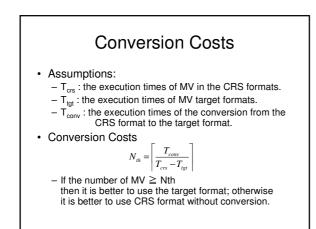
Speed-up ratios							
Number	of threads			4	8	16	32
Matrix	Format	1	2				
(-)	CRS	1.00	2.00	4.18	8.19	15.51	27.16
(a)	BSR_41	1.00	2.04	5.19	9.59	15.77	21.69
	CRS	1.00	1.90	3.99	7.93	14.23	24.14
(b)	BSR_22	1.00	1.88	3.91	9.42	15.90	25.18
(-)	CRS	1.00	1.95	3.82	8.03	15.13	26.50
(C)	BSR_41	1.00	1.93	3.83	10.60	18.75	28.03
())	CRS	1.00	1.93	3.63	7.00	14.91	28.07
(d)	BSR_41	1.00	1.91	3.45	7.34	19.22	32.21
(-)	CRS	1.00	1.99	3.97	7.70	14.61	30.72
(e)	BSR_41	1.00	1.97	3.83	7.04	14.73	33.63
	CRS	1.00	1.99	3.99	7.97	15.72	30.07
(f)	BSR_31	1.00	1.98	3.97	7.84	15.20	17.58
	DIA	1.00	2.00	4.03	10.88	37.84	63.51



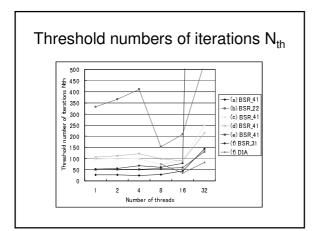




- The speed-ups have attained good results for any storage format when the FSB was dedicated to one CPU.
- The performance for the BSR format causes a great decrease when the FSB is shared with two CPUs.
- The cache and memory bus architectures have been observed to influence the optimum choice of the storage format.



Conversion times T_{conv} (in milliseconds)								
Number of threads				_				
Matrix	Format	1	2	4	8	16	32	
(a)	BSR_41	61.2	30.7	15.0	8.5	6.7	10.4	
(b)	BSR_22	96.9	50.8	24.9	12.4	7.7	8.5	
(C)	BSR_41	132.8	68.1	35.4	17.8	11.1	14.1	
(d)	BSR_41	247.6	132.3	69.8	35.9	20.2	22.2	
(e)	BSR_41	575.9	292.7	148.5	78.2	47.7	53.5	
(f)	BSR_31	3370.8	1720.3	1073.5	478.6	303.8	439.2	
	DIA	907.4	485.6	270.3	178.0	165.7	178.8	



Summary : Conversion Costs

- · The value of Nth changes slightly except (b).
- · The conversion of the storage format provides faster computation of the matrixvector product
 - If the number of the matrix-vector product is 100 times or more in this test matrices.

Conclusions (1)

- Our Implementations have attained satisfactory • scalability.
 - It is necessary to take into account the first-touch mechanism.
- The storage format has been observed to greatly affect the performance of matrix-vector products.
 - In order to maximize the performance of a machine, users must be able to choose an appropriate storage format for each matrix.
- The conversion of the storage format provides faster computation of the matrix-vector product If the number of the matrix-vector product is certain times or more.

Conclusions (2)

- · To take into account the First-touch mechanism.
 - we parallelized the storage format conversion routines using OpenMP.

Future Works

- · We are planning to port and to evaluate our codes to other shared memory parallel machines.
- Our next goal is parallelization for distributed memory parallel machines through MPI and MPI-OpenMP hybrid parallelization.
- We will also work toward high-performance iterative linear solvers using these kernel routines and effective preconditioners for the solvers.

Acknowledgements

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